LIMITATIONS







We saw many examples of regular languages Also sans equivalent representations by way of DFA/NFA/regex. Today we will look at the linitations of DFAs.





We will book at a variant of problem 14 from the tutovial sheet. Of λ is regular, so is $\lambda_f = 2\chi \chi \cdot \chi \in \lambda_f$ We have a DFA M for L. Somehow we want to extract an NFA for Ly from M. A general strategy for such problems is to think of flags on the states of M. What config do you start with? How do the flags move vort transitions? Where are the flags situated in accepting configs?

 $\chi_f = \int \chi | \chi \cdot \chi \in \mathcal{L}$ det $M = (Q, \Xi, \delta, q_0, F)$ be a DFA recognizing L. Put a green flag on 90, and guess some state 9, where we put two flags — one blue, and one red. Never more the red flag. Move the green and blue flags in lock step, according to the input letter. When do we accept?

Cau we now formally describe the NFA M' for L? $\mathcal{M}' = \left(\mathcal{Q}', \mathcal{Z}, \mathcal{A}, \mathcal{Q}_{o}, \mathcal{F}' \right)$ $Q' = Q \times Q \times Q$ ved $(q_1, q_2, q_3), \alpha, (q'_1, q'_2, q'_3)) \in \Delta$ iff $q'_{1} = \delta(q_{1}, a), q'_{2} = \delta(q_{2}, a), q'_{3} = q_{3}, \text{for } q_{1}, q_{2}, q_{3} \in \mathbb{Q}, a \in \mathbb{Z}$ $Q_0 = \left\{ \left(Q_0, Q_1, Q_1 \right) \mid Q \in Q^2 \right\}$ $f' = \left\{ (q, f, q) \right\} q \in \mathbb{Q}, f \in F_{\gamma}^{2}$ hove that $\lambda_f = \lambda(M')$.

So we showed that if
$$\lambda$$
 is regular, then $[x]xx$
Is the reverse true?
Is $\lambda = [x \cdot x] \times \epsilon \lambda_f$ regular, if λ_f is re-
Can I perform a Concat-like construction?
Hard to figure out where to break the string?
Suppose I add an actual separating character.
Is $\lambda_{nus} = fx \propto |x \epsilon d_f$ regular, where $\lambda_f \leq z^*$ an
What about $\lambda_k = [x \cdot x] \times \epsilon d_f$, $|x| \leq k_f$?
Does this help us narrow down the issue?

 $f(x) x \cdot x \in \mathcal{L}_{f}$ is regular.

f is regular? ion ?

string "in advance" acter.



The problem is to do with x being unboundedly long. How much can a DFA vennember? Essentially, just a state and a letter. Keeping toack of an unbounded string with no set pattern in order to match it against "future" letters is beyond a DFA!