## NON-CONTEXT FREE

LANGUAGES

Recall: We showed that some non-regular languages are context-free languages.

These are generated by context-free grammors, and recognized by pushdown automata.

Today

Context-free?

REGULAR

Is every non-regular language context-free?

## Closure properties:

-> We saw that CFIs are closed under intersection with regular languages (Cross-product construction, truch the stack only for the CH)

Are CFLs closed under union? If  $L_1$  and  $L_2$  are CFLs, is  $d_1 v d_2$  also a CFL?  $G_1 = (NT_1, T_1, R_1, S_1)$   $G_2 = (NT_2, T_2, R_2, S_2)$   $T = T_1 v T_2$ 

 $G = \left(NT_1 \cup NT_2 \cup \left\{S_1^2, T, R_1 \cup R_2 \cup \left\{S_3^2, S_1 \middle| S_2^2, S\right\}\right)$ S "fresh"

\* Which of the other regular operations is the class of CHs closed under?

Construct a CFG or a PDA for  $X = \{a^nb^nc^n \mid n > 0\}$   $X' : \{a^nb^{2n}a^n \mid n > 0\}$   $X_q = \{a^n^2 \mid n > 0\}$ 

$$\alpha'' = \left\{ \frac{2n}{n} \mid n > 0 \right\}$$

We said that DFAs could not "count" What Can PDAs not do? What CAN they do? Broadly, - They can count Is an  $a^{n^2}$  n > 0 a CFL? - They can keep track of pairs² Is fann n nzof a CAL?

- 1) Not beyond a "linear" count
- 2) But not if distinct pairs have an "overlap"

How does one show that a language is not context-free?