CONTEXT - FREE

ANGUAGES





Recall: A context-free grammar is a 4-type
where
NT: finite set of non-terminal symbols
T: finite set of terminal symbols
R: finite set of production rules, each
X::= s

$$\in NT$$
 $\in (NTUT)^*$
mby a single X
 S : start symbol, $S \in NT$
 $\mathcal{L}(G) = \mathcal{L}(G) = \mathcal{L}(G)$ S ::= ω via an application
of rules in R

G = (NT, T, R, S),

i rule of the form

r of a finite sequence?

rome CFG G is

'b's ? is context-free

eses.

CFGs is in parsing. ell-formed by rules which generates it.

Consider dab = 2 (20) (20 has an equal number of "a's and "b's g Lab is generated by the grammar $S = E \begin{bmatrix} aSb \\ bSa \end{bmatrix} SS$ Consider aabbab E La. How night this grammar generate it? Have to guess the rule which was applied to get this string, and continue recursively! fo suppose we got aabbab by using S = a.Sb. Now I need to check if the grammar can generate abba etc. The easiest way to keep track of this is via parse trees.



A grammor which com generate nultiple parse trees for a string is called ambiguous (other wise, unambiguous) The grammar S::= Elasbs bsas is also ambiguous

To remove ambiguity, one number somehow ensure

$$S ::= E | aBS | bAS$$

 $B ::= b | aBB$ needs to match two 'b's

 $A := \alpha | bAA$

Proving that a grammar is unambiguous can be difficult! Can sometimes do induction on strings in the language, but not always!

r that matches are unique.

against this 'a', then the rest against two already-read 'a's

needs to match two 'a's against two already-read 'b's

Much like we provided à machine model for regenes via DFAs/NFAs, we would like a machine model for CFGs as well. We said that DFAs count count, so there was no DFA for Lab, because recognizing Lab, intriviewely, required the machine to - count #'a's - count #`b's - check that these numbers were equal. What is a small extension me can do to a DFA/NFA so it can recognize Lab?

n Check whether it is zero.

this if ctr = 0

r a string w,

ind of finite automaton. due of the counter counter is zero.

For a language like $Apd = \frac{1}{2}\cos rev(\omega) \left| \cos \epsilon \leq \frac{\pi}{2} \right|$, it is not clear how to use a single counter to help recognize it. But what we want is that if we somehow guess the end of w, the letter we read last in w should also be the letter we read first in whatever follows, and that this inside-out matching continues till the end. A stack Could help us keep track of this!