

PRELIMINARIES

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AND

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INTRODUCTION

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# What should you already know? Discrete maths (COL202)

- \* Sets: Membership, equality, set operations, properties, inductive definitions, subsets, power sets, Cartesian products
- \* Relations: Composition, properties, closures
- \* Functions: Total/partial functions, in-/sur-/bi-jections, composition
- \* Cardinality: Finite vs infinite sets, countable vs uncountable, diagonalization
- \* Proof techniques: Induction (mathematical/structural) especially!

What is this course about?

Introduction to Automata and Theory of Computation

Why do we need a theory of computation?

To know what is computable, and what is not

If something is computable,

- How much computing machinery does it require?
- How efficiently can it be computed?

So how do we figure out whether something is computable?

What counts as a computation?

Need some uniform way to talk about computation.



We can describe a computation as a set of pairs of the form  
 $(\text{Input}, \text{Output})$  — skip if None / trivial

Such a set is called a language